

Fundamentele Informatica 3

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<http://www.liacs.nl/home/rvwvliet/f13/>

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Herhalend onderwerpen FI2

5. Pushdown Automata

5.1. Definitions and Examples

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- hoorcollege: maandag 6 feb - 14 mei; zaal 403, 13:45–15:30
- werkcollege: dinsdag 7 feb - 15 mei; zaal 403, 13:45–15:30 (Vouter Duivesteyn)

• boek: John C. Martin, Introduction to Languages and the Theory of Computation, **4th edition**
Er komt verwijsljst naar 3rd edition

- tentamens: maandag 11 juni 2012, 10:00–13:00
- maandag 20 augustus 2012, 10:00–13:00

• Drie huiswerkopgaven (individueel)
Niet verplicht, maar ...

eindcijfer = 0.9 × tentamencijfer + cijferhuiswerkopgaven

- 6 EC

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Fundamentele Informatica 2

2.1. Finite Automata

2.4. The Pumping Lemma

3.1. Regular Languages and Regular Expressions

3.2. Nondeterministic Finite Automata

3.3. The Nondeterminism in an NFA Can Be Eliminated

3.4/3.5. Kleene's Theorem

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Fundamentele Informatica 2

4.2. Context-Free Grammars

4.3. Regular Languages and Regular Grammars

4.4. Derivation Trees

6.1. The Pumping Lemma for Context-Free Languages

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5. Pushdown Automata

Stack in PDA contains symbols from certain alphabet.

Usual stack operations: pop, top, push

Extra possibility: replace top element X by string α

$\alpha = \Lambda$ pop
 $\alpha = X$ top
 $\alpha = YX$ push
 $\alpha = \beta X$ push*
 $\alpha = \dots$

Top element X is required to do a move!

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just like FA, PDA accepts strings / language
just like FA, PDA has states
just like FA, PDA reads input one letter at a time
unlike FA, PDA has auxiliary memory: a stack
unlike FA, by default PDA is nondeterministic
unlike FA, by default Λ -transitions are allowed in PDA

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Example 5.3. A PDA Accepting the Language $AnBn$

$$AnBn = \{a^i b^i \mid i \geq 0\}$$

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Definition 5.10. A Deterministic Pushdown Automaton

A pushdown automaton $M = (Q, \Sigma, \Gamma, q_0, Z_0, A, \delta)$ is *deterministic* if it satisfies both of the following conditions.

1. For every $q \in Q$, every $\sigma \in \Sigma \cup \{\Lambda\}$, and every $X \in \Gamma$, the set $\delta(q, \sigma, X)$ has at most one element.
2. For every $q \in Q$, every $\sigma \in \Sigma$, and every $X \in \Gamma$, the two sets $\delta(q, \sigma, X)$ and $\delta(q, \Lambda, X)$ cannot both be nonempty.

A language L is a *deterministic context-free language* (DCFL) if there is a deterministic PDA (DPDA) accepting L .

2. (In other words): For every $q \in Q$ and every $X \in \Gamma$, if $\delta(q, \Lambda, X)$ is not empty, then $\delta(q, \sigma, X)$ is empty for every $\sigma \in \Sigma$.

5.2. Deterministic Pushdown Automata