

Compilerconstructie

najaar 2013

<http://www.liacs.nl/home/rvvliet/coco/>

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college 9, dinsdag 26 november 2013

Code Optimization

9.2 Introduction to Data-Flow Analysis

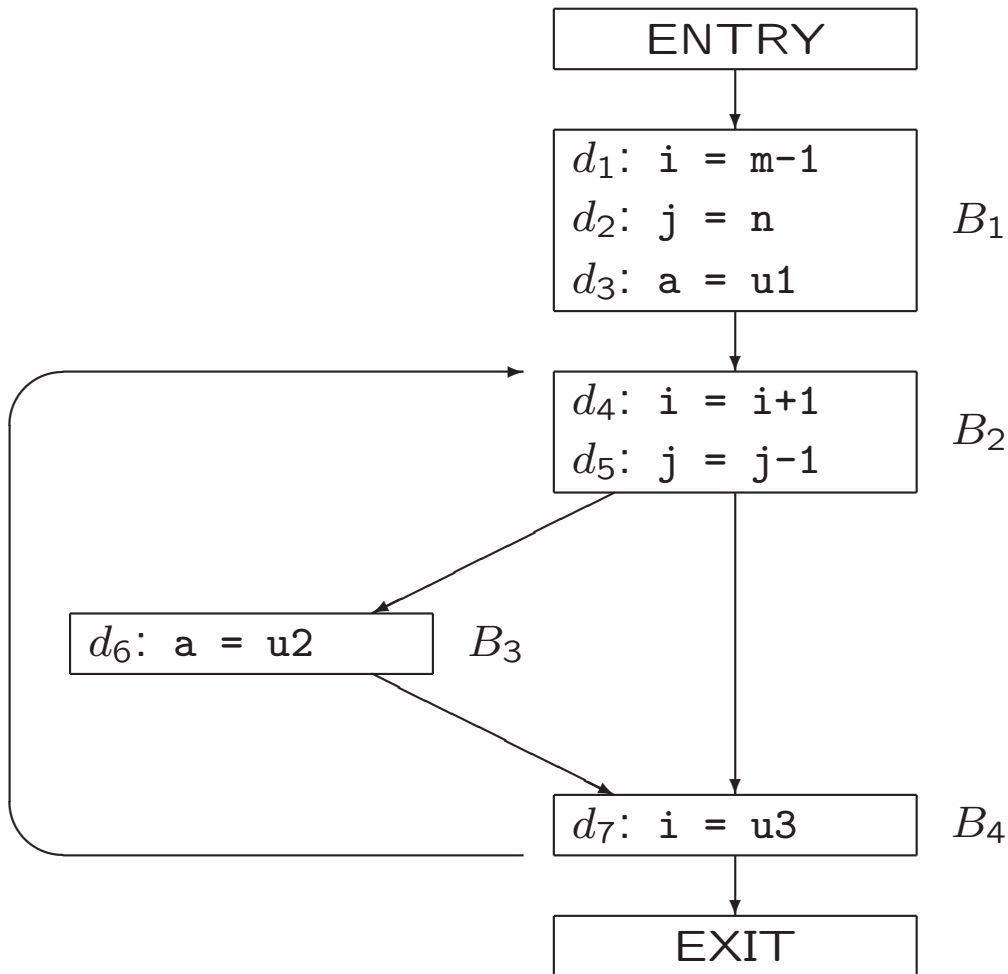
- Optimizations depend on [data-flow analysis](#), e.g.,
 - Global common subexpression elimination
 - Dead-code elimination
- [Execution path](#) yields program state
- Extract information from program state for data-flow analysis
- Usually infinite number of execution paths / program states
- Different analyses extract different information

Data-Flow Analysis (Examples)

Extract information from program states at **program point**

- **Reaching definitions:** which definitions (assignments of values) of variable a reach program point?
Useful for debugging
- Can variable x only have one constant value at program point?
Useful for constant folding

Computing Reaching Definitions



Reaching definitions

- Before B_1 : \emptyset
- After B_1 : $\{d_1, d_2, d_3\}$
- Before B_2 : \dots

Data Flow Values

- $IN[s]$: before statement s
- $OUT[s]$: after statement s
- Transfer function f_s
 - forward: $OUT[s] = f_s(IN[s])$
 - backward: $IN[s] = f_s(OUT[s])$

Computing Reaching Definitions

- Effect of single definition $d : u = v \text{ op } w$:
 - $\text{OUT}[d] = \{d\} \cup (\text{IN}[d] - \dots)$

Computing Reaching Definitions

Effect of single definition $d : u = v \text{ op } w$:

- $\text{OUT}[d] = \{d\} \cup (\text{IN}[d] - \{\text{all other definitions of } u \text{ in program}\})$

- Hence,

$$\begin{aligned} f_d(x) &= \{d\} \cup (x - \{\text{all other definitions of } u \text{ in program}\}) \\ &= \text{gen}_d \cup (x - \text{kill}_d) \end{aligned}$$

where

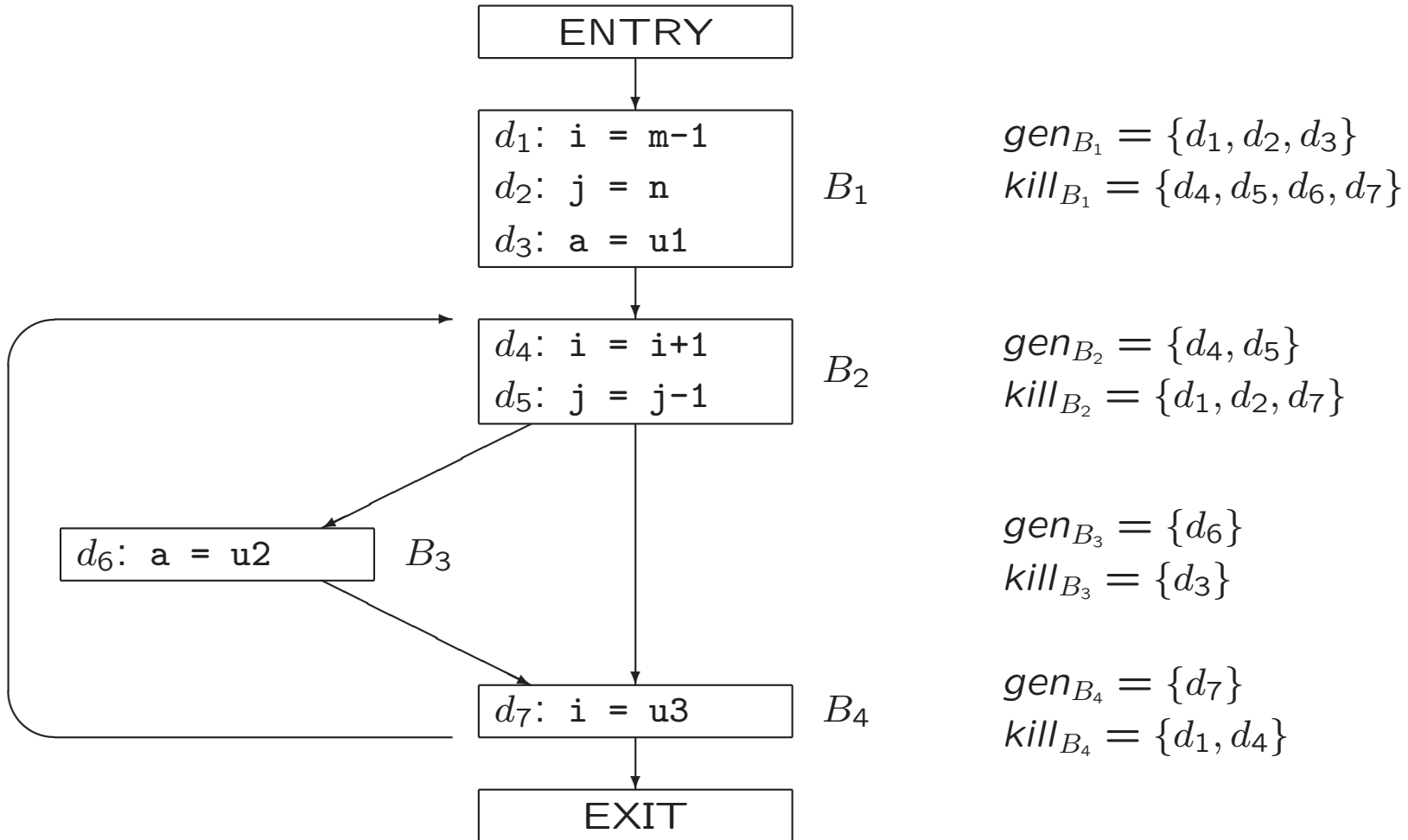
$$\begin{aligned} \text{gen}_d &= \{d\} \\ \text{kill}_d &= \{\text{all other definitions of } u \text{ in program}\} \end{aligned}$$

Computing Reaching Definitions

Effect of block B , with definitions $1, 2, \dots, n$:

$$\begin{aligned} gen_B &= \{n, n-1, \dots, 1\} - \{ \text{definitions killed afterwards} \} \\ &= gen_n \cup (gen_{n-1} - kill_n) \cup (gen_{n-2} - kill_{n-1} - kill_n) \dots \\ kill_B &= kill_1 \cup kill_2 \cup \dots \cup kill_n \end{aligned}$$

Computing Reaching Definitions



Iterative Algorithm for Computing Reaching Definitions

```
OUT[ENTRY] =  $\emptyset$ 
for each basic block  $B$  other than ENTRY
    OUT[ $B$ ] =  $\emptyset$ 

while (changes to any OUT occur)
    for each basic block  $B$  other than ENTRY
    {   IN[ $B$ ] =  $\cup_{\text{predecessors } P \text{ of } B} \text{OUT}[P]$ 

        OUT[ $B$ ] =  $gen_B \cup (\text{IN}[B] - kill_B)$ 
    }
```

Typical form of algorithm for forward data-flow analysis

Example with $B = B_1, B_2, B_3, B_4, \text{EXIT} \dots$

Implementation of Iterative Algorithm for Computing Reaching Definitions

With bit vectors

Block B	$\text{OUT}[B]^0$	$\text{IN}[B]^1$	$\text{OUT}[B]^1$	$\text{IN}[B]^2$	$\text{OUT}[B]^2$
B_1	000 0000	000 0000	111 0000	000 0000	111 0000
B_2	000 0000	111 0000	001 1100	111 0111	001 1110
B_3	000 0000	001 1100	000 1110	001 1110	000 1110
B_4	000 0000	001 1110	001 0111	001 1110	001 0111
EXIT	000 0000	000 0000	001 0111	001 0111	001 0111

Live-Variable Analysis

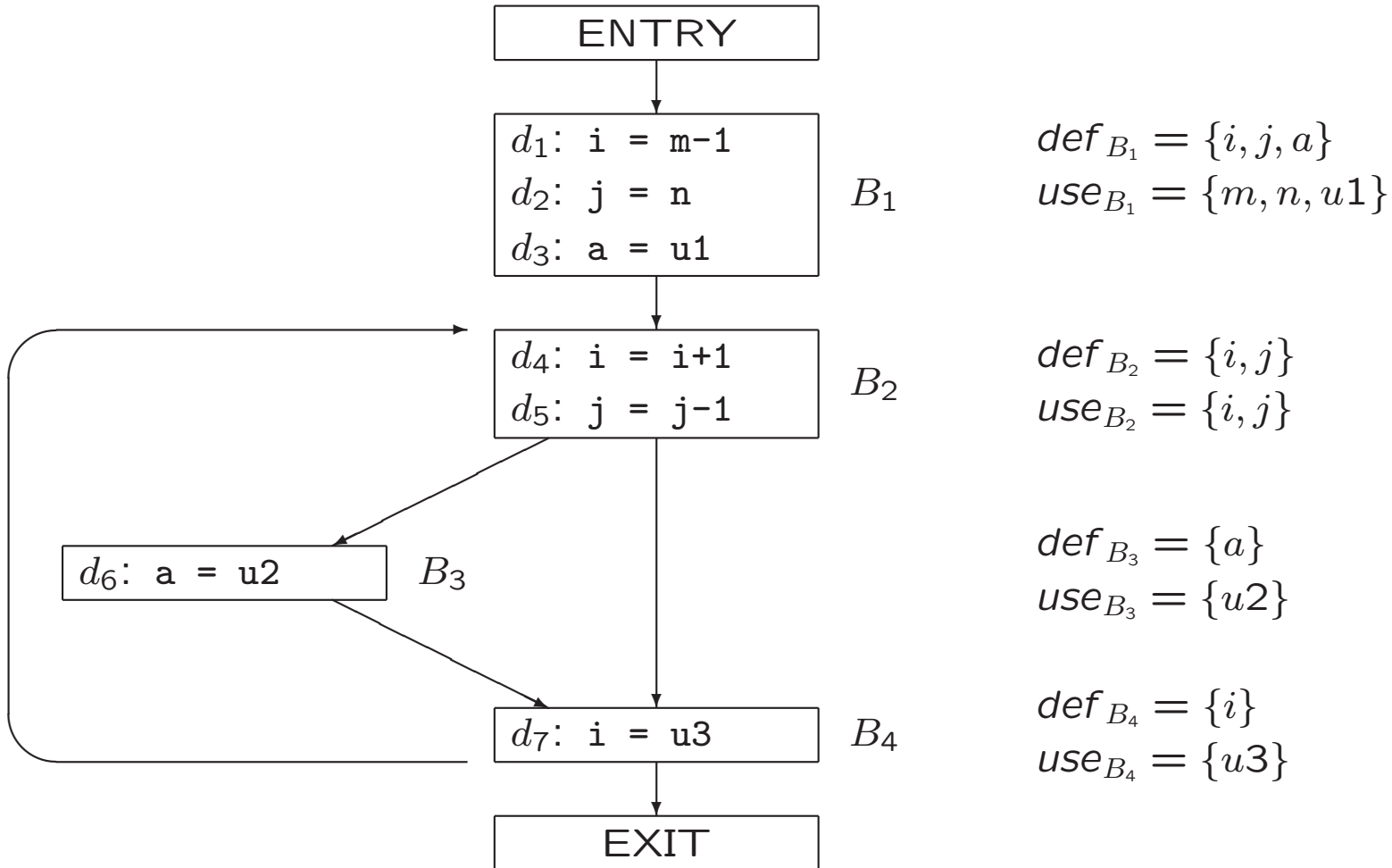
- Variable x is **live** at program point p ,
if value of x at p could be used later along *some* path
- Otherwise x is **dead** at p
- Information useful for register allocation (see college 7)
- Information about later use must be propagated backwards

Live-Variable Analysis

Effect of block B on live variables

- def_B : variables *defined* in B
- use_B : variables that may be *used* in B prior to any definition in B

Computing Liveness



Iterative Algorithm for Computing Liveness

$IN[EXIT] = \emptyset$

for each basic block B other than EXIT

$IN[B] = \emptyset$

while (changes to any IN occur)

for each basic block B other than EXIT

{ $OUT[B] = \cup_{\text{successors } S \text{ of } B} IN[S]$

$IN[B] = use_B \cup (OUT[B] - def_B)$

}

Typical form of algorithm for backward data-flow analysis

Available expressions

- Is (value of) expression $x \text{ op } y$ available?
- Useful for global common subexpression elimination
- Can be decided with data-flow analysis

Available Expressions (Example)

Computing Available Expressions (Example)

Statement	Available Expressions
	\emptyset
$a = b + c$	$\{b + c\}$
$b = a - d$	$\{a - d\}$
$c = b + c$	$\{a - d\}$
$d = a - d$	\emptyset

Computing Available Expressions

$OUT[ENTRY] = \emptyset$

for each basic block B other than ENTRY

$OUT[B] = U$

while (changes to any OUT occur)

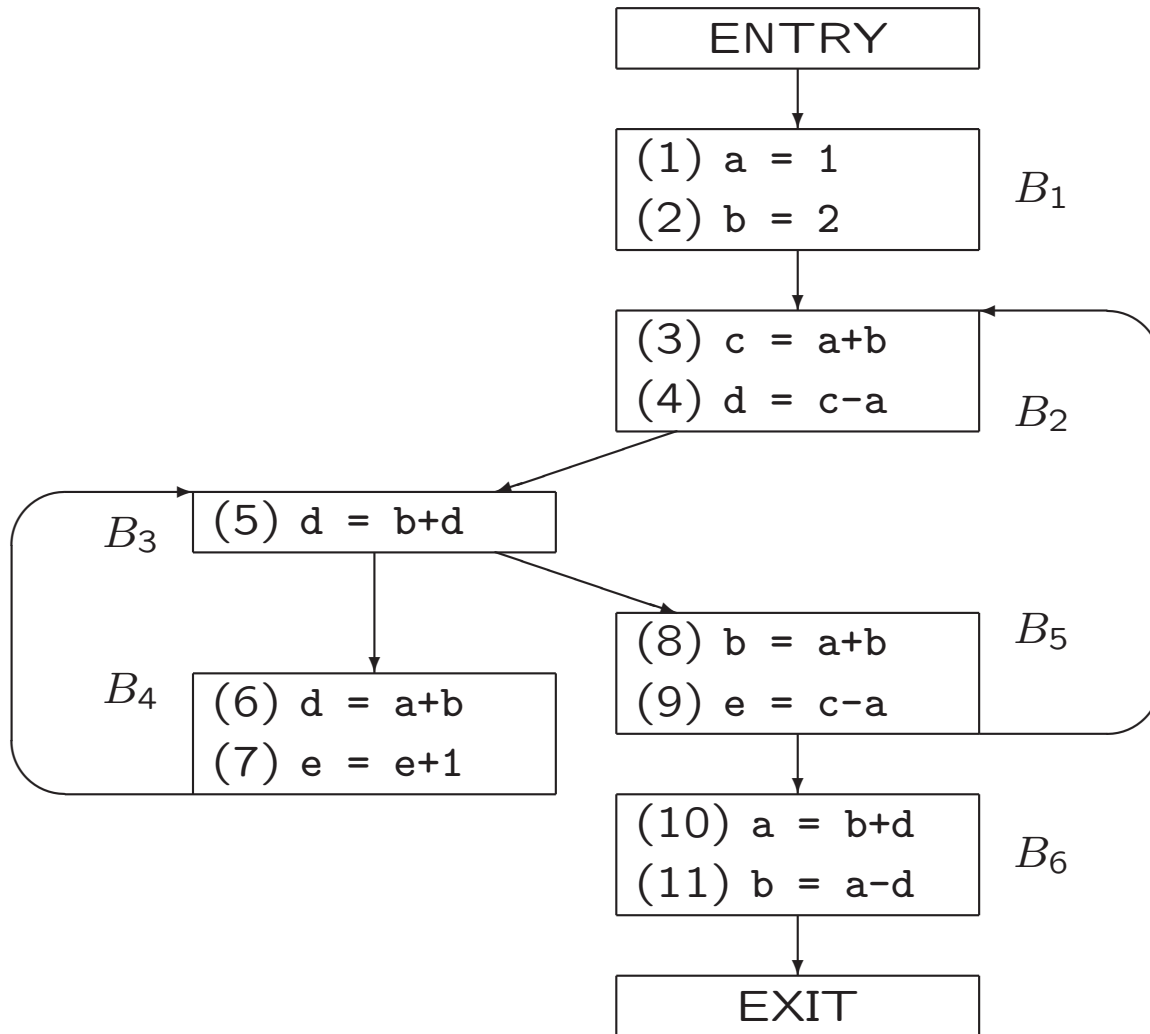
for each basic block B other than ENTRY

{ $IN[B] = \bigcap_{\text{predecessors } P \text{ of } B} OUT[P]$

$OUT[B] = e_gen_B \cup (IN[B] - e_kill_B)$

}

Flow Graph For Data Flow Analysis



Efficient Iterative Data-Flow Analysis

Example: computing reaching definitions

$OUT[ENTRY] = \emptyset$

for each basic block B other than ENTRY

$OUT[B] = \emptyset$

while (changes to any OUT occur)

for each basic block B other than ENTRY

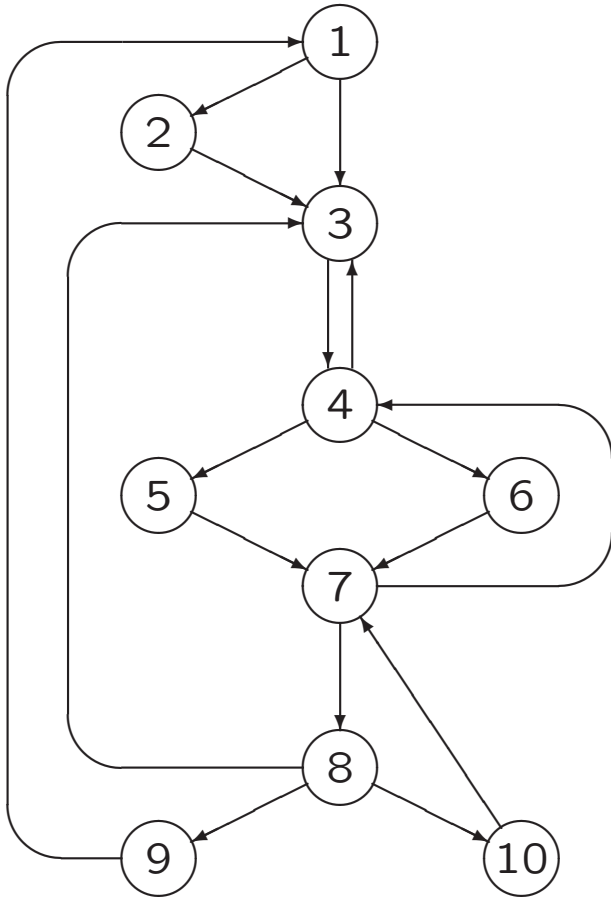
$IN[B] = \cup_{\text{predecessors } P \text{ of } B} OUT[P]$

$OUT[B] = gen_B \cup (IN[B] - kill_B)$

 }

Order of blocks in second for-loop matters

Efficient Iterative Data-Flow Analysis



Order of blocks in second for-loop matters

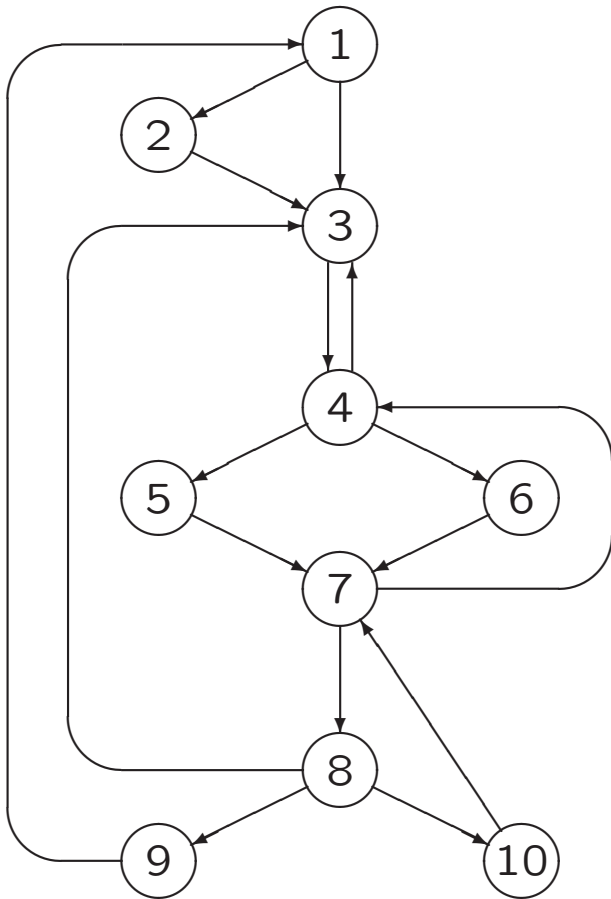
9.6 Loops in Flow Graphs

- Optimizations of loops have significant impact
- Essential to identify loops
- Used in region based analysis (not for exam)

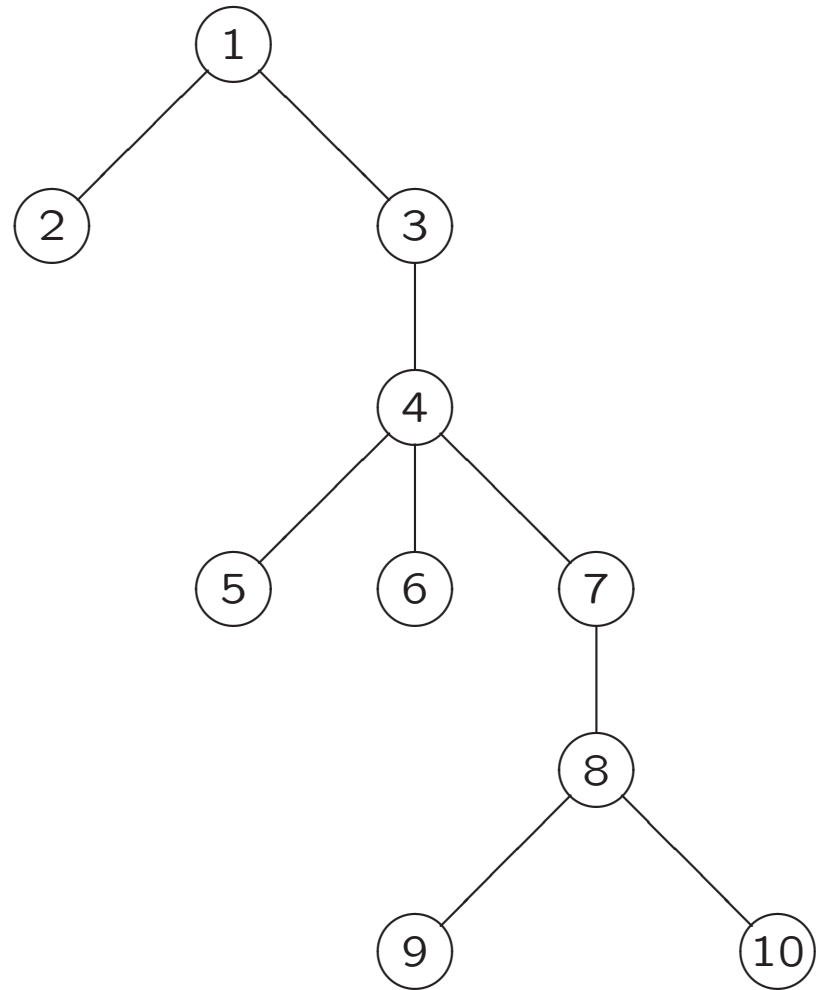
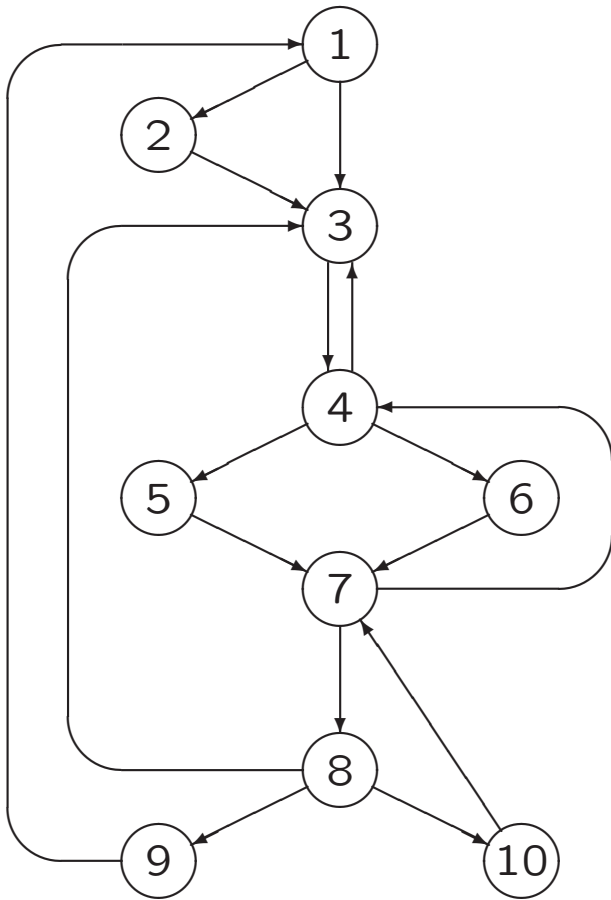
Dominators

- Dominators:
 - Node d dominates node n if every path from ENTRY node to n goes through d : $d \text{ dom } n$
 - Node n dominates itself
 - Loop entry dominates all nodes in loop
- Immediate dominator m of n :
last dominator on (any) path from ENTRY node to n
 - if $d \neq n$ and $d \text{ dom } n$, then $d \text{ dom } m$

Dominators (Example)



Dominator Trees (Example)



Finding Dominators

Forward data-flow analysis

N is set of all nodes

$OUT[ENTRY] = \{ENTRY\}$

for each node n other than ENTRY

$OUT[n] = N$

while (changes to any OUT occur)

for each node n other than ENTRY

{ $IN[n] = \bigcap_{\text{predecessors } m \text{ of } n} OUT[m]$

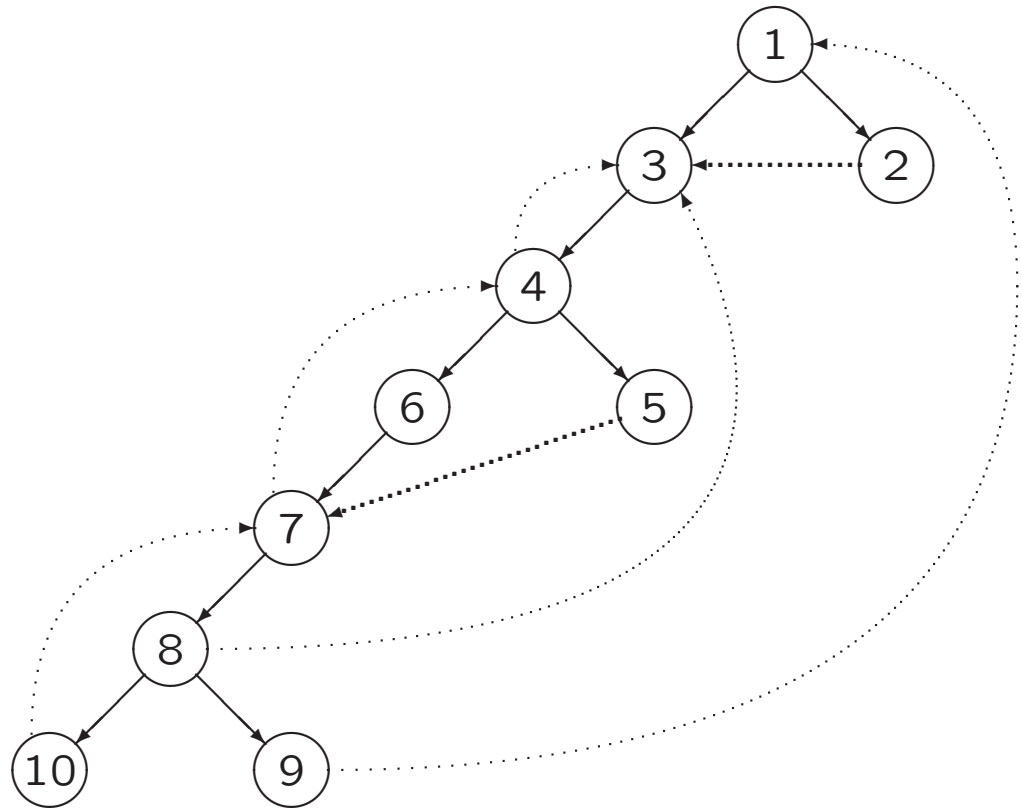
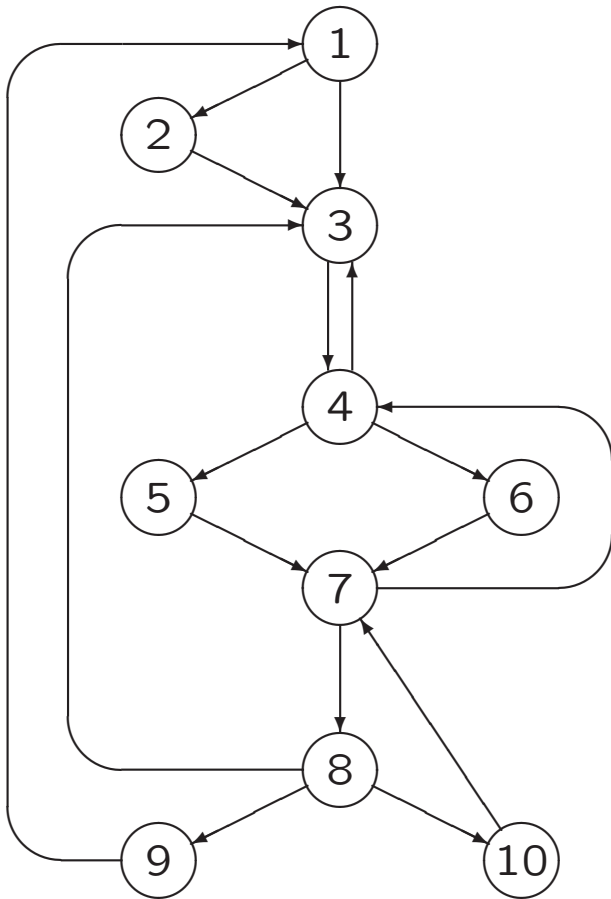
$OUT[n] = IN[n] \cup \{n\}$

}

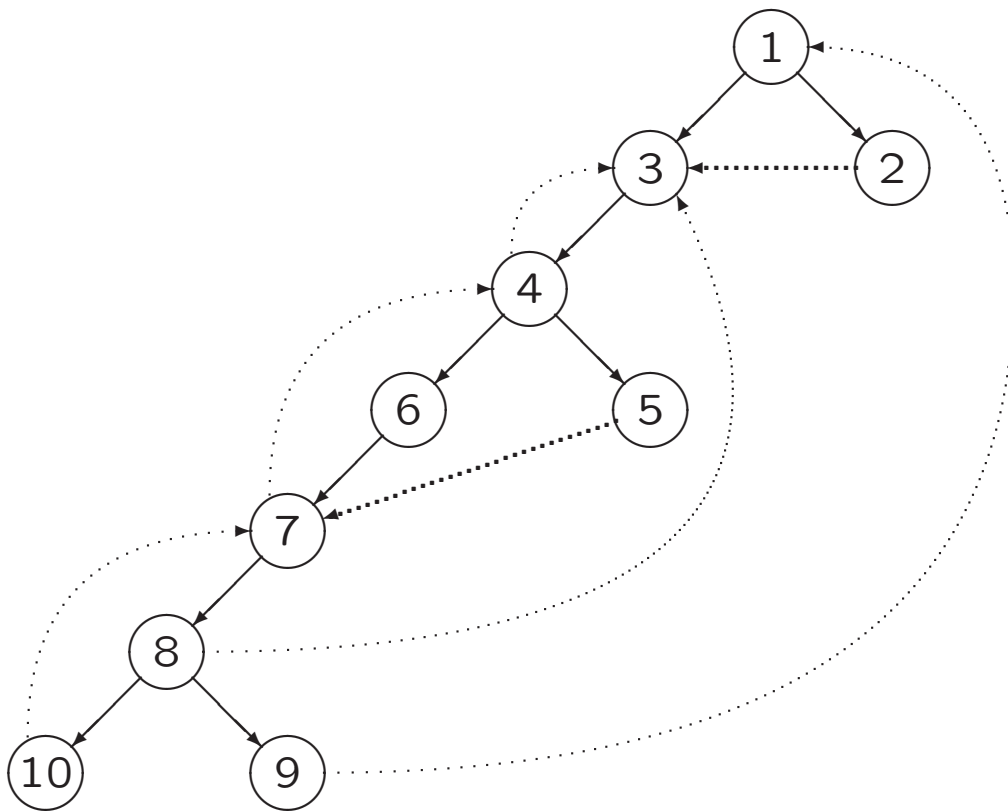
Depth-First Traversal

- Depth-first traversal of graph
 - Start from entry node
 - Recursively visit neighbours (in any order)
 - Hence, visit nodes far away from the entry node as quickly as it can (DF)

A Depth-First Spanning Tree



A Depth-First Spanning Tree



- Advancing edges
- Retreating edges
- Cross edges
- Back edge $a \rightarrow b$,
if b dominates a
(regardless of DFST)
- Each back edge is
retreating edge in DFST
- Flow graph is **reducible**,
if each retreating edge in
any DFST is back edge

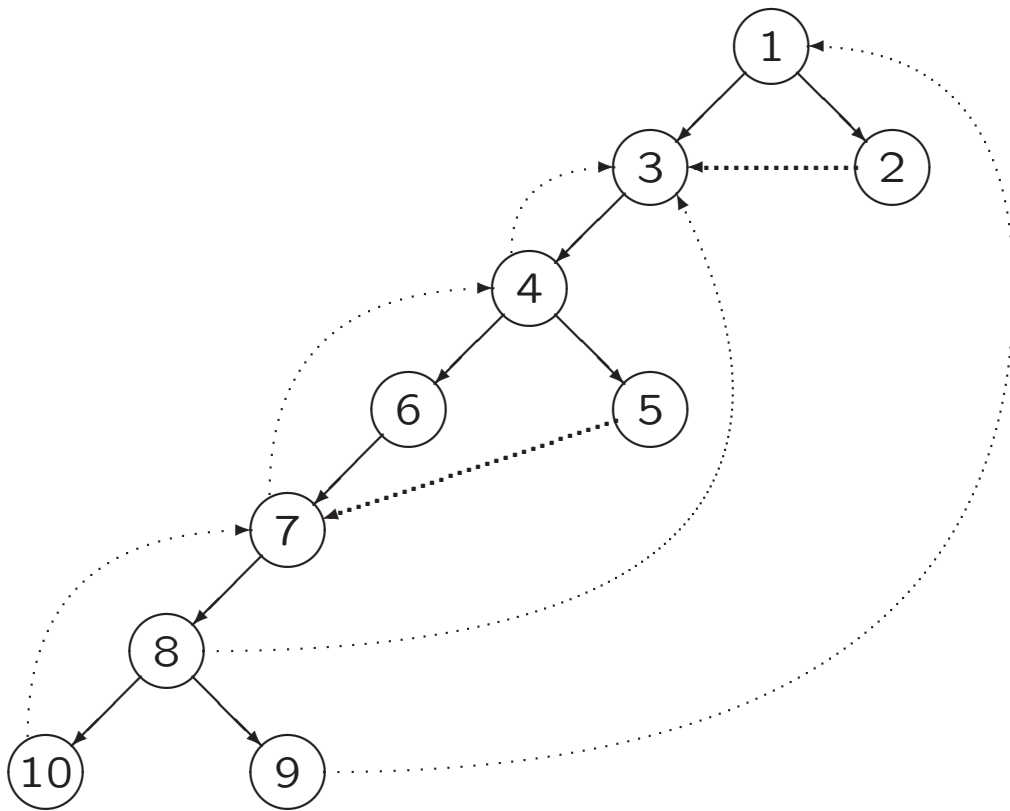
(Non)Reducible flow graphs

- In practice, almost every flow graph is reducible
- Example of nonreducible flow graph
(with advancing edges)
- To decide on reducibility:
 1. Remove back edges
 2. Is remaining graph acyclic?

Natural loops

- If loop has single-entry node, then compiler can assume certain initial conditions
- Natural loop
 1. Has single-entry node: header
 2. Has back edge to header
- Each back edge $n \rightarrow d$ determines natural loop, consisting of
 - d
 - all nodes that can reach n without going through d
- Constructing natural loop of back edge...

Natural Loops (Example)



No Natural Loops

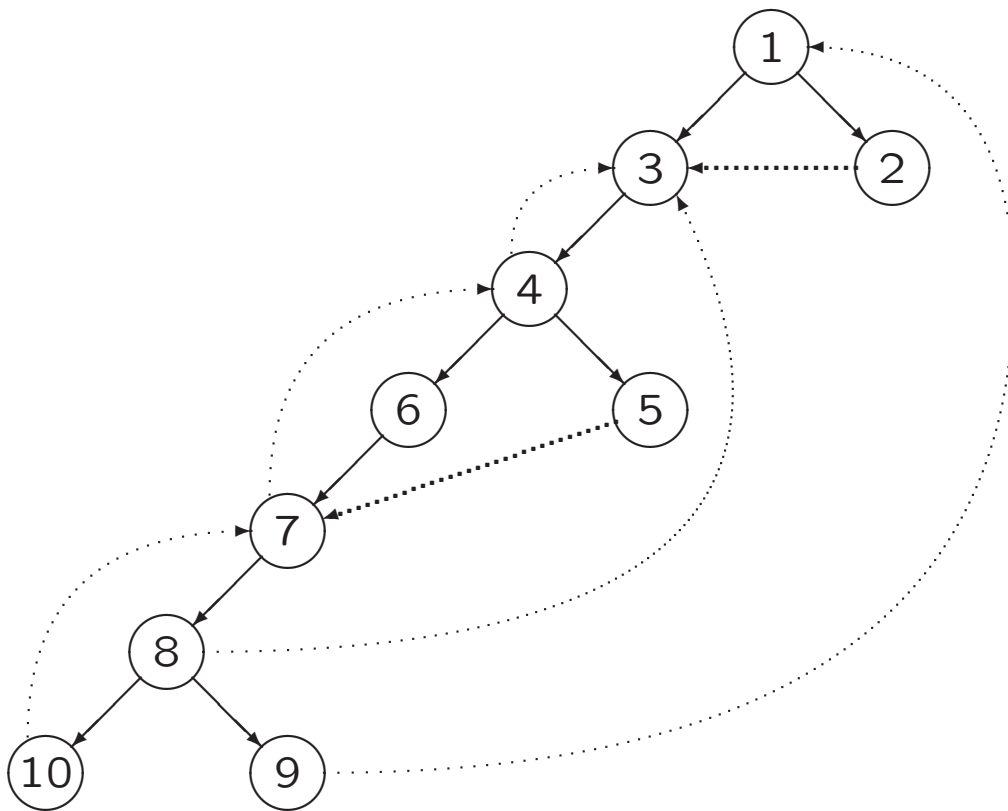
Natural Loops

- Useful property: unless two natural loops have same header
 - either they are disjoint
 - or one is nested within other

Allows for inside-out optimization

- Assumption: if necessary, combine natural loops with same header...

A Depth-First Ordering

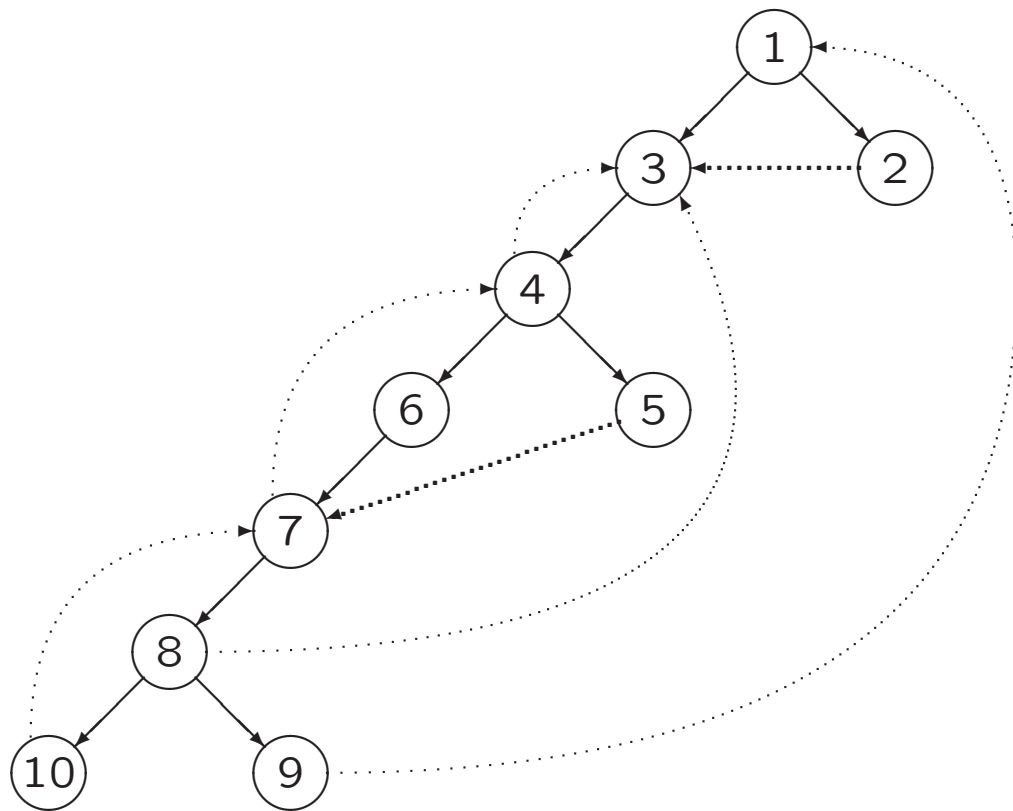


- **Depth-First Ordering:**
nodes in DFST
in WRL order \approx
reverse of postorder
- Example:
1,2,3,4,5,6,7,8,9,10
- Edge $m \rightarrow n$ is
retreating, if and only if
 n comes before m
in depth-first ordering

Depth of Flow Graph

- **Depth** of DFST is largest number of retreating edges on any cycle-free path
- If flow graph is reducible, then depth is independent of DFST:
depth of flow graph
- $\text{Depth} \leq \text{depth of loop nesting in flow graph}$

Depth of Flow Graph (Example)



Depth is 3, because of path
 $10 \rightarrow 7 \rightarrow 4 \rightarrow 3$

Speed of Convergence of Iterative Data-Flow Algorithms

In data-flow analysis, can significant events be propagated to node along acyclic path?

- Yes for
 - Reaching definitions
 - Live-variable analysis
 - Available expressions
- No for
 - Copy propagation

If yes, then fast convergence possible

Efficient Iterative Data-Flow Analysis

Example: computing reaching definitions

$OUT[ENTRY] = \emptyset$

for each basic block B other than ENTRY

$OUT[B] = \emptyset$

while (changes to any OUT occur)

for each basic block B other than ENTRY

$IN[B] = \cup_{\text{predecessors } P \text{ of } B} OUT[P]$

$OUT[B] = gen_B \cup (IN[B] - kill_B)$

 }

Order of blocks in second for-loop matters

Fast Convergence

- Forward data-flow problem: visit nodes in depth-first-order
- Recall: edge $m \rightarrow n$ is retreating, if and only if n comes before m in depth-first ordering
- Example: path of propagation of definition d :

3 \rightarrow 5 \rightarrow 19 \rightarrow 35 \rightarrow 16 \rightarrow 23 \rightarrow 45 \rightarrow 4 \rightarrow 10 \rightarrow 17

- Number of iterations: $1 + \text{depth} (+ 1)$
- Typical flow graphs have depth 2.75
- Backward data-flow problem: visit nodes in reverse of depth-first-order

En verder...

- Dinsdag 3 december: practicum over opdracht 4
- Maandag 9 december: inleveren opdracht 4
- Dinsdag 17 december, 10:00–13:00: tentamen
- Vragenuur ?

Compiler constructie

college 9

Code Optimization

Chapters for reading:

9.2, 9.6