

SemCom

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## **Seminar Combinatorial Algorithms**

Walter Kusters, Universiteit Leiden

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`www.liacs.nl/home/kusters/semcom/`

Who is Knuth?

<http://www-cs-faculty.stanford.edu/~knuth/>



T<sub>E</sub>X, Dancing Links, ...

We use the following book(let):

Donald E. Knuth,  
The Art of Computer Programming, Volume 4,  
Combinatorial Algorithms;  
Fascicle 1, Bitwise Tricks & Techniques, Binary De-  
cision Diagrams,  
Pearson, 2009

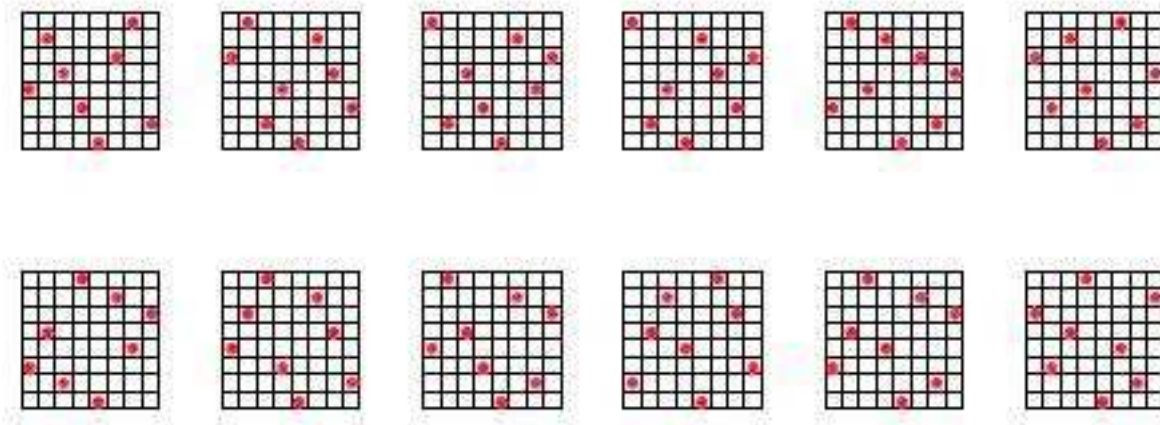


See also <http://www.cs.utsa.edu/~wagner/knuth/index.html>.

In the second half of the seminar we will probably discuss papers from our  $n$ -Queens bibliography:

<http://www.liacs.nl/home/kosters/nqueens/>

These 322 papers all try —each in its own way— to place  $n$  queens on a chessboard, in such a way that no queen attacks another.



First half: act as chairman during discussion of Section 7.1.4 from the book, dealing with **Binary Decision Diagrams**.

Make a few slides, and heavily use the blackboard.

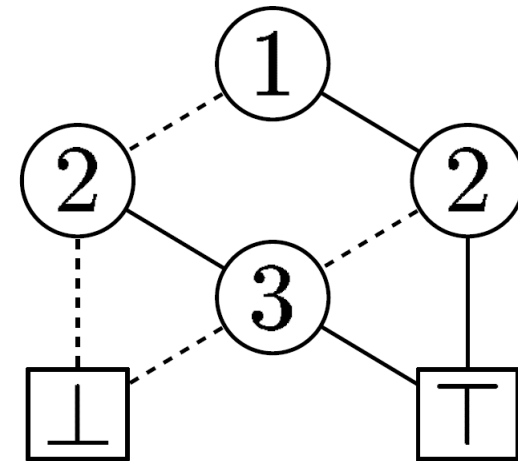
Second half: present  **$n$ -Queens** paper in one hour. Make several slides, and hardly use the blackboard.

For both: make a 5–10 page **report** in L<sup>A</sup>T<sub>E</sub>X/PDF.

[pages 70–73 from the book]

Binary Decision Diagrams (BDDs) are used to represent Boolean functions.

BDDs must be ordered and reduced.



A Boolean function  $f(x_1, \dots, x_n)$  gives rise to a truth table of order  $n$ : the binary string with its  $2^n$  values — in proper order. A bead of order  $n$  is a truth table that is *not* a square.

The nodes of a Boolean function's BDD are in one-to-one correspondence with its beads, i.e., its subtables that are beads.