Robotics

Erwin M. Bakker| LIACS Media Lab

11-2 2020



Universiteit Leiden

Bij ons leer je de wereld kennen



• It is necessary to be at every class and to complete every workshop.

Overview

- Robotic Actuators
- Configuration Space
- Rigid Body Motion
- Forward Kinematics
- Inverse Kinematics
- Link: <u>http://modernrobotics.org</u>



K.M. Lynch, F.C. Park, Modern Robotics: Mechanics, Planning and Control, Cambridge University Press, 2017

Universiteit Leiden. Bij ons leer je de wereld kennen























How to move to a goal?

Problem: How to move to a goal?

• Grasp, Walk, Stand, Dance, Follow, etc.

Solution:

- 1. Program step by step
- Computer Numerical Control (CNC), Automation.
- 2. Inverse kinematics:
- take end-points and move them to designated points.
- 3. Tracing movements
 - by specialist, human, etc.
- 4. Learn the right movements
 - **Reinforcement Learning**, give a reward when the movement resembles the designated movement.



https://pybullet.org/wordpress/

Universiteit Leiden. Bij ons leer je de wereld kennen

Configuration Space

Robot Question: Where am I?

Answer:

The robot's configuration: a specification of the positions of all points of a robot.

Here we assume:

Robot links and bodies are rigid and of known shape => only a few variables needed to describe it's configuration.



K.M. Lynch, F.C. Park, Modern Robotics: Mechanics, Planning and Control, Cambridge University Press, 2017



Configuration Space

Assume we have a coin with 3 points A, B, C on it.

In the plane A,B,C have 6 degrees of freedom:

$(x_A, y_A), (x_B, y_B), (x_C, y_C)$

A coin is rigid => 3 extra constraints on distances: d_{AB} , d_{AC} , d_{BC} are fixed, wherever the location of the coin would be.



- 1. The coin and hence A can be placed everywhere $=> (x_A, y_A)$ free to choose.
- 2. B can only be placed under the constraint that its distance to A would be equal to d_{AB} . => freedom to turn the coin around A with angle ϕ_{AB} => (x_A , y_A , ϕ_{AB}) are free to choose.
- 3. C should be placed at distance d_{AC} , d_{BC} from A and B, respectively => only 1 possibility, hence no degree of freedom added.

Degrees of Freedom (DOF) of a Coin

- = sum of freedoms of the points number of independent constraints
- = number of variables number of independent equations = 6 3 = 3

Configuration Space

[1] Definition 2.1.

The **configuration** of a robot is a complete specification of the position of every point of the robot.

The minimum number *n* of real-valued coordinates needed to represent the configuration is the number of **degrees of freedom** (**dof**) of the robot.

The *n*-dimensional space containing all possible configurations of the robot is called the **Configuration Space** (**C-space**).

The configuration of a robot is represented by a point in its C-space.

Universiteit Leiden. Bij ons leer je de wereld kennen



Open-chain robot: Manipulator (in V-REP). [1]



Closed-chain robot: Stewart-Gough platform. [1]

Degrees of Freedom of a Robot

 A rigid body in 3D Space has 6 DOF



- A joint can be seen to put constraints on the rigid bodies it connects
- It also allows freedom to move relative to the body it is attached to.





Degrees of Freedom of a Robot

• A rigid body in 3D Space has 6 DOF



- A **joint** can be seen to put constraints on the rigid bodies it connects
- It also allows freedom to move relative to the body it is attached to.

L	Revolute (R) Prismatic (P) Helical (H)		;		Cylindrical (C) Universal (U) Spherical (S)
			Constraints c		Constraints c
			between two		between two
Joint type		dof f	$_{\rm planar}$		spatial
			rig	id bodies	rigid bodies
Revolute (R)		1	2		5
Prismatic (P)		1	2		5
Helical (H)		1	N/A		5
Cylindrical (C)		2	N/A		4
Universal (U)		2	N/A		4
Spherical (S)		3	N/A		3
					. <u> </u>

Planar Mechanism DOF = 4

N = 5 links

J = 4 joints

 $f_i = 1$, for all i $c_i=2$, for all i

Universiteit Leiden. Bij ons leer je de wereld kennen

Degrees of Freedom of a Robot

Proposition (Grübler's formula)

Consider a mechanism consisting of

- N links, where ground is also regarded as a link.
- J number of joints,
- m number of degrees of freedom of a rigid body (m = 3 for planar mechanisms and m = 6 for spatial mechanisms),
- f_i the number of freedoms provided by joint i, and
- c_i the number of constraints provided by joint i, where $f_i + c_i = m$ for all i.

Then Grübler's formula for the number of degrees of freedom of the robot is

$$dof = m(N-1) - \sum_{i=1}^{J} c_i = m(N-1-J) + \sum_{i=1}^{J} f_i$$

This formula holds only if all joint constraints are independent. If they are not independent then the formula provides a lower bound on the number of degrees of freedom.







C-Spaces

- The C-space of a rigid body in the plane can be written as $\mathbb{R}^2 \times S^1$, since the configuration can be represented as the concatenation of the coordinates (x, y) representing \mathbb{R}^2 and an angle θ representing S^1 .
- The C-space of a PR robot arm can be written $\mathbb{R}^1 \times S^1$ (We will occasionally ignore joint limits, i.e., bounds on the travel of the joints, when expressing the topology of the C-space; with joint limits, the C-space is the Cartesian product of two closed intervals of the line.)
- The C-space of a 2R robot arm can be written $S^1 \times S^1 = T^2$, where T^n is the *n*-dimensional surface of a torus in an (n + 1)-dimensional space. (See Table 2.2.) Note that $S^1 \times S^1 \times \cdots \times S^1$ (*n* copies of S^1) is equal to T^n , not S^n ; for example, a sphere S^2 is not topologically equivalent to a torus T^2 .
- The C-space of a planar rigid body (e.g., the chassis of a mobile robot) with a 2R robot arm can be written as $\mathbb{R}^2 \times S^1 \times T^2 = \mathbb{R}^2 \times T^3$
- As we saw in Section 2.1 when we counted the degrees of freedom of a rigid body in three dimensions, the configuration of a rigid body can be described by a point in R³, plus a point on a two-dimensional sphere S², plus a point on a one-dimensional circle S¹, giving a total C-space of R³ × S² × S¹.



Task Space and Work Space



Figure 2.12: Examples of workspaces for various robots: (a) a planar 2R open chain; (b) a planar 3R open chain; (c) a spherical 2R open chain; (d) a 3R orienting mechanism

The **workspace** is a specification of the configurations that the end-effector of the robot can reach.

Universiteit Leiden. Bij ons leer je de wereld kennen



The SCARA robot is an RRRP open chain that is widely used for tabletop pick-and-place tasks. The end-effector configuration is completely described by (x, y, z, φ)

 \Rightarrow task space $R^3 x S^1$ and

 \Rightarrow **workspace** as the reachable points in (x, y, z), since all orientations φ can be achieved at all reachable points.

Rigid Body Motion

Rigid-body position and orientation (x, y, z, ϕ , θ , ψ)

- Can also be described by 4x4 matrix with 10 constraints.
- In general 4x4 matrices can be used for
 - Location
 - Translation + rotation of a vector or frame
 - Transformation of coordinates between frames
- Velocity of a rigid body: $(\partial x/\partial t, \partial y/\partial t, \partial z/\partial t, \partial \phi/\partial t, \partial \theta/\partial t, \partial \psi/\partial t)$

Exponential coordinates:

Every rigid-body configuration can be achieved by:

- Starting in the fixed home frame and integrating a constant twist for a specified time.
- Direction of a screw axis and scalar to indicate how far the screw axis must be followed









Rigid Body Motions in the Plane





Rigid Body Motions in the Plane



16





Figure 4.2: Illustration of the PoE formula for an *n*-link spatial open chain.

Inverse Kinematics Which angles θ_1 , and θ_1 will lead to location (x,y)?



(a) A workspace, and lefty and righty (b) Geometric s configurations.

Figure 6.1: Inverse kinematics of a 2R planar open chain.

In general: IK-Solvers

Law of cosines gives: $L_1^2 + L_2^2 - 2L_1L_2 \cos \beta = x^2 + y^2$

, hence

 $\beta = \cos^{-1}\left(\frac{L_1^2 + L_2^2 - x^2 - y^2}{2L_1L_2}\right)$

 $\alpha = \cos^{-1} \left(\frac{x^2 + y^2 + L_1^2 - L_2^2}{2L_1 \sqrt{x^2 + y^2}} \right)$

Answer: $\theta_1 = \gamma - \alpha, \quad \theta_2 = \pi - \beta$

,and similarly

 $\gamma = atan2(y,x)$

Universiteit Leiden. Bij ons leer je de wereld kennen



Robotics Homework I

Assignment:

Give a link to the coolest, strangest, most impressive, most novel, or technologically inspirational robot you could find.

Due: Monday 10-2 at 14.00 PM.

Email your link to erwin@liacs.nl with subject 'Robotics'.

Universiteit Leiden. Bij ons leer je de wereld kennen

Robotics Homework II

Assignment:

Visit <u>http://modernrobotics.org</u> and obtain the pdf of the <u>book</u>. Read Chapters 1 and 2 and answer the following exercises:

- 2.7
- 2.9 for Figures 1.18 d, e, and f
- 2.17 a) and b).

Due: Thursday 28-2 at 14.00 PM.

Email your answers to erwin@liacs.nl with subject 'Robotics HW2'.

Robotics Preparations

1) Form YetiBorg Racing Teams of 3 to 4 people Appoint one person who will be responsible for the robot.

Email your teams to <u>erwin@liacs.nl</u> with subject 'Robotics YetiBorg Racing Team'. **Due:** Thursday 7-3 at 14.00 PM.

2) Project Proposal Title and Abstract

Give the title and abstract of the project proposal you will present on March 15^{th} . Also mention the number of people that will cooperate on the project (1-4).

Email your proposal to <u>erwin@liacs.nl</u> with subject 'Robotics Project Proposal'. **Due:** Thursday 7-3 at 14.00 PM.

Universiteit Leiden. Bij ons leer je de wereld kennen

References

- 1. K.M. Lynch, F.C. Park, Modern Robotics: Mechanics, Planning and Control, Cambridge University Press, 2017. (DOI: 10.1017/9781316661239)
- 2. https://pybullet.org/wordpress/

Robotics



Bij ons leer je de wereld kennen

Robotics in the News

- Jimmy Drogtrop: <u>https://www.youtube.com/watch?v=sqOPnPVTJ74</u>, <u>https://www.youtube.com/watch?v=sKjAp0iZ7dc</u>
- Sartana Fitra Amir, swarm robotics for agricultural application. <u>http://laral.istc.cnr.it/saga/</u>
- Chen Wang, <u>https://www.youtube.com/watch?v=6vYA8L_r850</u>
- Simon van Wageningen: spotmini from boston: <u>https://www.youtube.com/watch?v=aFuA50H9uek</u> <u>https://www.youtube.com/watch?v=7rgFtkMiXms</u>
- Cailin Dagg: Following are the "coolest" robots I found:
 - A bipedal robot that combines walking and flying to navigate: Article <u>https://newatlas.com/leonardo-robot-walks-flies/58165/</u>
 - A bio-inspired robot that navigates using polarised sunlight and step-counting : Article <u>https://www.wired.com/story/a-6-legged-robot-stares-at-the-sky-to-navigate-like-a-desert-ant/</u> Paper <u>http://robotics.sciencemag.org/content/4/27/eaau0307</u>
 - A robot built to examine the locomotion of early tetrapods: Article <u>https://www.wired.com/story/a-crocodile-like-robot-helps-solve-a-300-million-year-mystery/</u> Paper <u>https://www.nature.com/articles/s41586-018-0851-2</u>

 Online Simulator <u>https://biorob2.epfl.ch/pages/Orobates_interactive/</u>
- Giovanni Calore, <u>https://www.youtube.com/watch?v=W1LWMk7JB80</u>. (SpotMini Boston Dynamics)

Robotics in the News

- Mathé Hertogh: These two examples I found really cool: <u>https://confluence.acfr.usyd.edu.au/display/AGPub/Our+Robots</u> <u>https://www.kickstarter.com/projects/rse/worlds-first-eco-robot-protecting-reefs-from-lionf/description</u>
- Jeroen Rook: <u>https://www.oreilly.com/ideas/building-structures-with-robot-swarms</u> Broad applications for construction, but also within agriculture. <u>https://sydney.edu.au/engineering/our-research/robotics-and-intelligent-systems/australian-centre-for-field-robotics/agriculture-and-the-environment.html</u>
- Pedro Santamaria: In my opinion Sony's Aibo <u>https://us.aibo.com/</u>
- Maxime Casara: ABB robot: <u>https://www.youtube.com/watch?v=SOESSCXGhFo</u>

Universiteit Leiden. Bij ons leer je de wereld kennen

Robotics in the News

- Luca Ballan: 9 robots developed by Boston Dynamics <u>https://www.youtube.com/watch?v=bRHG7YObDuU</u>
- Sophie Hendrikse:
 - <u>https://robots.ieee.org/robots/aibo2018/</u>
 - <u>http://news.mit.edu/2019/robot-jenga-0130</u>
 - https://techcrunch.com/2016/05/31/robots-date-mate-and-procreate-3d-printed-offspring-in-robot-baby-project/
 - <u>https://techcrunch.com/wp-content/uploads/2016/05/robot-baby-bgw-1.jpg?w=591</u>

 Koen Putman Going to start with an obvious one, but the work of Simone Giertz is lovely: <u>https://www.youtube.com/channel/UC3KEoMzNz8eYnwBC34RaKCQ/</u>
 I will never forget the banana peel slip in the Spot Mini introduction. <u>https://youtu.be/tf7IEVTDjng</u> It's also just a really great robot. And I've always thought robot pets for companionship are interesting. <u>https://www.bbc.com/news/av/technology-35321227/</u> They're not really there yet though. The more recent Anki Vector also has a sort of buddy role and personality. <u>https://www.anki.com/en-us/vector</u>
 Laurens Arp:

 Biological 'nanobots', used for medical purposes: Research paper: <u>https://www.nature.com/articles/nbt.4071</u> Quick article: <u>https://www.ft.com/content/57c9f432-de6d-11e7-a0d4-0944c5f49e46</u>

Robotics in the News

- Renaie Leveridge: <u>https://wyss.harvard.edu/robotic-insect-walks-on-water/</u>
- Abdullah Alsaubie: <u>https://www.anki.com/en-us/vector/vector-helpful</u>
- Roos Doekemeijer:
 - Toddler-like exploring and learning: <u>https://www.youtube.com/watch?v=NOLAwD4ZTW0</u>
 - Hive mind controlled by drone https://www.youtube.com/watch?v=i3ernrkZ91E
 - Just for fun: pancake-making machine: <u>https://www.youtube.com/watch?v=W_gxLKSsSIE</u>
- Reinis Nudiens: Boston Dynamics robots: <u>https://www.youtube.com/watch?v=LikxFZZO2sk</u>
- Micky Faasen:
 - The Djedi-robot for pyramids research:
 - <u>https://www.euronews.com/2015/07/23/robot-tries-to-unlock-giza-pyramid-s-secrets</u>
 <u>https://www.newscientist.com/article/mg21028144-500-first-images-from-great-pyramids-chamber-of-secrets/</u>
 - Another one: https://news.artnet.com/art-world/tiny-robot-egyptian-pyramids-1180052
- Alexander Mulkidzhanyan: <u>https://www.youtube.com/watch?v=8t8fyiiQVZ0</u>
- Mei Chen: Kengoro from Japan: <u>https://www.youtube.com/watch?v=3FlzxKuqzUM</u>
- L.M. Vos: <u>https://www.youtube.com/watch?v=kHBcVlqpvZ8</u>